# Fusion of Color Photometric Stereo Method and Slit Pattern Projection Method to Measure Three-Dimensional Shapes of a Human Face 

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#### Abstract

We propose a new method for measuring three-dimensional (3D) moving facial shapes. This method uses photometric stereo method and slit pattern projection method with color light sources. The time required for sampling data can be reduced by switching the color light rays at high speed, and hence a series of 3D shapes of a moving human face at each instant can be measured. Experimental results are shown to demonstrate the feasibility of the proposed method.


## 1 Introduction

The human face is one of the most important parts of the human body because it has great expressive ability that can provide clues to the personality and the emotions of a person. Recently, automatic and non-contact facial analysis systems with video cameras and computers have been used in many applications. To analyze a human face correctly, the 3D shapes of the human face must be measured accurately.

In most of the existing methods, such as the binocular stereo method $[1,2]$, the 3D coordinates of objects are measured directly using two cameras. In such methods, the greatest difficulty is the identification of corresponding points of the images. The slit pattern projecting method simplifies the identification problem. By projecting points or lines onto a face, we can compute the 3D coordinates of the illuminated positions. To measure the entire face by the projecting method, the scanning method has been applied $[3,4,5,6]$. This method, however, requires a lot of time to scan the entire face and the face should be kept motionless during the scan. Thus, the measuring time should be as short as possible to avoid errors due to changes in the shape of the face.

For rapid measurement, the use of a silicon range finder has been proposed [7]. This method can provide 3D coordinates at high speed. However, it requires special hardware for scanning the object, leading to a high production cost. Color-coded light stripes enable instantaneous measurement of the entire facial shape $[8,9]$. The accuracy of the measured data, however, is low because it is affected by the color of the skin.

Recently, several methods of measuring the normal vectors of objects based on photometric properties, such as the shape from shading method [10, 11], and
photometric stereo method [12, 13], have been proposed. These methods can provide a high density of 3D information about complicated object shapes in a short time. These methods, however, cannot be used to measure the 3D shapes of a human face accurately. We have integrated slit pattern projection method into photometric stereo method using a conventional video camera and measured the 3D shapes of a face accurately $[14,15]$. However, this method uses only gray scale images and requires more than three images for the measurement.

In this paper, a new method of measuring a series of 3D facial shapes is introduced. This method uses a conventional video camera, two point light sources with red filters, and a slit pattern projector with a blue filter. The red light rays are projected onto a face at minute time intervals by switching the two point light sources, while the multiple blue light stripes are projected onto the face by the slit pattern projector all the time. We can measure the 3D facial shapes from the two images accurately by using the color information of each image. By switching the point light sources at high speed, the 3D shapes of a moving human face can be measured.

## 2 Method of Measurement

Fig. 1 shows the apparatus and the 3 D orthogonal coordinate system for the proposed 3D measurement. A video camera is set in front of a face. The origin of the coordinate system is the center of the camera lens. The $x$-axis is parallel to the axis of the abscissa of the camera image plane and the $y$-axis is parallel to the axis of the ordinate of the plane. Two point light sources $\left(S_{1}, S_{2}\right)$ and a slit pattern projector are arranged on a straight line that is parallel to the $y$-axis. Two red filters are set in front of the point light sources and one blue filter is set in front of the slit pattern projector.

With the apparatus, the proposed method is composed of five steps: (1) separation of facial images into two shading images and a slit image, (2) computation of normal vectors, (3) depth measurement by projecting stripes, (4) integration of normal vectors inside finite intervals, and (5) blending of curved segments.

### 2.1 Separation of Facial Images

Two point light sources $S_{1}$ and $S_{2}$ are switched in turn to illuminate the face, while a slit pattern projector illuminates the face all the time. The 3D facial shape at a particular instant is measured from two facial images. These images illuminated by each light source are obtained using the video camera. $I_{S_{1} L}$ is the facial image illuminated by $S_{1}$ and the slit pattern projector. $I_{S_{2} L}$ is the facial image illuminated by $S_{2}$ and the slit pattern projector. These images are color images described by

$$
\begin{align*}
I_{S_{1} L} & =\left(R_{S_{1} L}, G_{S_{1} L}, B_{S_{1} L}\right),  \tag{1}\\
I_{S_{2} L} & =\left(R_{S_{2} L}, G_{S_{2} L}, B_{S_{2} L}\right), \tag{2}
\end{align*}
$$



Fig. 1. Two point light sources $S_{1}$ and $S_{2}$ are switched in turn to illuminate the face, while a slit pattern projector illuminates the face all the time. (a) The face is illuminated by $S_{1}$ and the slit pattern projector. (b) The face is illuminated by $S_{2}$ and the slit pattern projector.
where $R_{S_{k} L}, G_{S_{k} L}$, and $B_{S_{k} L}$ are red component, green component, and blue component of $I_{S_{k} L}(\mathrm{k}=1,2)$, respectively.

The face is illuminated by the point light and slit pattern at the same time. To distinguish between these light sources, we make sure that the range of the transmittance of the red/blue filter does not overlap with the range of blue/red sensitivity of the camera. Fig. 2 shows the ranges of the transmittance of the filters and the sensitivity of the camera in our system. The red component of the facial image corresponds to the intensity of point light sources $S_{1}$ and $S_{2}$, and the blue component of the facial image corresponds to the intensity of the slit pattern projector. With the apparatus, we separate the two facial images into two shading images $I_{S_{1}}$ and $I_{S_{2}}$ and a slit image $I_{L}$ as follows:

$$
\begin{equation*}
I_{S_{1}}=R_{S_{1} L}, \quad I_{S_{2}}=R_{S_{2} L}, \quad I_{L}=B_{S_{1} L} \tag{3}
\end{equation*}
$$

$I_{S_{1}}$ and $I_{S_{2}}$ are used as the intensity of radiance in subsection 2.2. $I_{L}$ is used as the slit image in subsection 2.3.

### 2.2 Computation of Normal Vectors

The normal vectors at all the points on the face are computed by the photometric stereo method [12]. In the conventional photometric stereo method, three light sources are necessary. In our system, only two light sources, $S_{1}$ and $S_{2}$, are used and they are switched at high speed to measure the vectors rapidly (Fig. 1). Two shading images of the face, $I_{S_{1}}$ and $I_{S_{2}}$, illuminated by the corresponding light source, are obtained by the separation method described in subsection 2.1. From


Fig. 2. Relative sensitivity of the video camera and transmittance of the red and blue filters.
the two images, one of the components ( $y$ component) of each normal vector on the face is determined by solving the Lambertian reflectance map. This method can provide a high density of information about the facial shape in a short time.

First, the normal vector $\mathbf{N}(x, y)$ at the point $(x, y, z)$ on the face is described by

$$
\begin{equation*}
\mathbf{N}(x, y)=\left(N_{x}(x . y), N_{y}(x, y), 1\right) . \tag{4}
\end{equation*}
$$

Assuming that the light sources are far from the face, relative to the size of the face, the direction to each light source can be specified by a fixed vector. Two vectors, $\mathbf{S}_{\mathbf{1}}$ and $\mathbf{S}_{\mathbf{2}}$, which point in the direction from the point $(x, y, z)$ to the light sources $S_{1}$ and $S_{2}$, respectively, are described by

$$
\begin{equation*}
\mathbf{S}_{1}=\left(0, S_{1_{y}}, 1\right), \quad \mathbf{S}_{2}=\left(0, S_{2_{y}}, 1\right) \tag{5}
\end{equation*}
$$

Assuming the Lambertian reflectance map, the following two equations are given:

$$
\begin{align*}
& E_{S_{1}}(x, y)=e_{S_{1}} R \frac{\mathbf{S}_{\mathbf{1}} \cdot \mathbf{N}(x, y)}{\left\|\mathbf{S}_{\mathbf{1}}\right\|\|\mathbf{N}(\mathbf{x}, \mathbf{y})\|}  \tag{6}\\
& E_{S_{2}}(x, y)=e_{S_{2}} R \frac{\mathbf{S}_{\mathbf{2}} \cdot \mathbf{N}(x, y)}{\left\|\mathbf{S}_{\mathbf{2}}\right\|\|\mathbf{N}(\mathbf{x}, \mathbf{y})\|}, \tag{7}
\end{align*}
$$

where $e_{S_{k}}$ is the intensity of incident illumination from $S_{k}$ filtering through the red filters, $E_{S_{k}}(x, y)$ is the intensity of radiance at the point $(x, y)$ illuminated by $S_{k}(k=1,2)$, and $R$ is the reflectance factor. The intensity $e_{S_{k}}$ is set a priori and the intensity $E_{S_{k}}(x, y)$ is obtained from the pixel values of the two shading images $I_{S_{k}}(x, y)(k=1,2)$.

From these equations, $N_{y}(x, y)$ is derived as

$$
\begin{equation*}
N_{y}(x, y)=\frac{1-\alpha}{S_{2_{y}} \alpha-S_{1_{y}}}, \quad \alpha=\frac{E_{S_{1}}(x, y) e_{S_{2}}\left\|\mathbf{S}_{\mathbf{1}}\right\|}{E_{S_{2}}(x, y) e_{S_{1}}\left\|\mathbf{S}_{\mathbf{2}}\right\|} \tag{8}
\end{equation*}
$$

### 2.3 Depth Measurement by Projecting Stripes

To obtain the boundary condition of integration, the proposed method uses the light projection method, i.e., multiple light stripes are projected onto the face using the slit pattern projector (Fig. 1) [16, 17]. The algorithm for the measurement is as follows:

1. Multiple light stripes are projected onto the face from one direction with the slit pattern projector.
2. The slit image $I_{L}$ is obtained from the separation described in subsection 2.1.
3. Bright regions are extracted by thresholding the image.
4. The 3D coordinates of the points on the extracted bright regions are computed by the stereo vision algorithm.

Let $P_{i}=\left(x_{i}, y_{i}, z_{i}\right)(i=1,2,3, \cdots)$ be the points on the intersection of the face and the light plane $L P_{j}$. The coordinates $\left(x_{i}, y_{i}, z_{i}\right)$ of $P_{i}$ are computed from the following equations:

$$
\begin{equation*}
\left(l_{j_{x}}, 1.0, l_{j_{z}}\right) \cdot\left(x_{i}, y_{i}, z_{i}\right)=-d_{j}, \quad x_{i}=\frac{x_{i}^{0}}{f} z_{i}, \quad y_{i}=\frac{y_{i}^{0}}{f} z_{i} \tag{9}
\end{equation*}
$$

where $f$ is the focal length of the camera, $\left(x_{i}^{0}, y_{i}^{0}\right)$ are the coordinates of the intersection point of the image plane and the line passing through both the camera lens center and $P_{i}$, and Eq.(9) represents the plane $L P_{j}$.

### 2.4 Integration of Normal Vectors inside Finite Intervals

To reconstruct the 3D curved segment, we integrate the surface normals $\mathbf{N}(x, y)$ computed by the photometric stereo method in subsection 2.2. For the integration, the region of the face is projected onto the $x y$-plane and divided into small domains (Fig. 3).

Let $P_{i}$ be the point on the light stripes on the face and the coordinates $\left(x_{i}, y_{i}, z_{i}\right)$ of $P_{i}$ be measured by the method described in subsection 2.3. Let the point $C_{i}=\left(x_{i}, y_{i}\right)$ be the projection of the measured point $P_{i}=\left(x_{i}, y_{i}, z_{i}\right)$ on the $x y$-plane. Fig. 4 shows the domain $D_{i}$ of integration. The domain $D_{i}$ is a two-dimensional finite interval centered at the point $C_{i}$ on the $x y$-plane. The interval is parallel to the $y$-axis and the length of the interval is $2 L_{i}$. To compute $z$ coordinates at the point $\left(x_{i}, y\right)$ in the domain $D_{i}$, that is $Z_{i}\left(x_{i}, y\right)$, the following equation is used:

$$
Z_{i}(x, y)=\left\{\begin{array}{cc}
z_{i}-\int_{y_{i}}^{y} N_{y}\left(x_{i}, Y\right) d Y & \left(x=x_{i}\right)  \tag{10}\\
0 & \left(x \neq x_{i}\right)
\end{array}\right.
$$



Fig. 3. Division of the sur- Fig. 4. The domain of inte- Fig. 5. Surface blending gration. procedure.

### 2.5 Blending of Curved Segments

Since multiple light stripes are used, several projected points $C_{i}$ have the same $x$ coordinates. The integration domains are overlapped in several regions, such as $D_{i}$ and $D_{j}$ in Fig. 5, and the integrated values $Z_{i}$ and $Z_{j}$, even on the same $y$ coordinates, may not be the same in the different domains. Therefore, computed curved segments in the overlapped regions of the domains are blended using infinitely differentiable functions.

In each domain $D_{i}$, the blending function $h_{i}$ is given as follows [18]:

$$
\begin{gather*}
\quad h_{i}(x, y)= \begin{cases}a\left(\frac{L_{i}-\left|y-y_{i}\right|}{L_{i}}\right) & \left(\text { if } \quad\left|y-y_{i}\right|<L_{i} \text { and } x=x_{i}\right) \\
0 & (\text { otherwise }),\end{cases}  \tag{11}\\
\text { where } a(t)=\left\{\begin{array}{cl}
0 & (t \leq 0) \\
\frac{b(t)}{b(t)+b(1-t)} & (0<t<1) \\
1 & (1 \leq t)
\end{array}\right.
\end{gather*}
$$

Clearly, the function $h_{i}(x, y)$ is infinitely differentiable. Now, the surface $Z(x, y)$ is computed as follows:

$$
\begin{equation*}
Z(x, y)=\frac{\sum_{i} h_{i}(x, y) Z_{i}(x, y)}{\sum_{i} h_{i}(x, y)} \tag{12}
\end{equation*}
$$

where $Z_{i}(x, y)$ are the $z$ coordinates of the segment at $(x, y)$ in the domain $D_{i}$.

## 3 Experiments

Fig. 6 shows the experimental apparatus and Fig. 7 shows two facial images taken by the conventional video camera. In these images, a subject is illuminated by the light sources $S_{1}, S_{2}$, and the slit pattern projector. The distance between the light sources and the subject face is about 3.0 meters. All the light rays are in the visible spectrum range and they do not have any adverse effects on human beings. The size of the two facial images is $640 \times 480$ pixels. Fig. 8 shows the separated three images, i.e. two shading images and one slit image. Fig. 9 shows the 3D facial shape obtained from the separated images. The two light sources are switched on in turn at a rate of 15 times per second. The facial images of the subject are taken at a rate of 15 frames per second using the video camera. Therefore, a series of 3D facial shapes at 15 frames per second can be measured. The measuring time can be reduced by using a high-speed video camera and by synchronizing image capturing with light switching. The computation time for obtaining a facial shape at an instant is about 10 seconds in total on a personal computer with a 1 GHz cpu. This time can be reduced by using a parallel processing method for computing normal vectors and integrating the vectors. As shown in Fig. 10, the time sequence of the 3D facial shapes is obtained from the time sequence of the images. Fig. 11 shows the selected time sequence of the measured 3D facial shapes.


Fig. 6. Experimental apparatus


Fig. 7. (a) Facial image $I_{S_{1} L}$ (b) Facial image $I_{S_{2} L}$


Fig. 8. (a) Shading image $I_{S_{1}}$ (b) Shading image $I_{S_{2}}$


Fig. 9. 3D facial shape.

## Time



Fig. 10. Time sequence of the measurement process.


Fig. 11. Time sequence of 3D facial shapes.

## 4 Evaluation of the Proposed Method

The proposed method is evaluated by measuring the 3D facial shapes of 20 motionless subjects using both the proposed method and another accurate method simultaneously and comparing the coordinates measured by the two methods. To obtain accurate 3D coordinates, the binocular stereo method is employed, and the corresponding points in the two images taken by the two cameras are identified manually. The $z$ coordinates on the bridge of the nose where the shape is most confusing have the largest margin of error.

The maximum error of 20 subjects in the regions between two light stripes illuminated by the slit projector is smaller than 3 mm , while the maximum error on the upper end (head) or lower end (chin) of the face is smaller than 7 mm .

## 5 Summary and Conclusions

In this paper, we introduced a new method for measuring 3D shapes of a moving human face. This method uses two point light sources with red filters, a slit pattern projector with a blue filter, and a conventional video camera. The point light sources are switched in turn to illuminate the face, while the slit pattern projector illuminates the face all the time. All the light rays are in the visible spectrum range and they do not have any adverse effects on human beings. With the apparatus, a series of 3 D facial shapes can be measured at 15 frames per second. Even if the human face moves and changes, detailed 3D facial shapes at a particular instant can be measured accurately.

The 3D deformations of the facial shapes are obtained from the time sequence of the measured 3D facial shapes. Moreover, the time sequence of the texture on the face is also obtained from the intensity of the facial image. The measuring time can be reduced by using a high-speed video camera and by synchronizing image capturing with light switching. As a further possible improvement of the system, the use of infrared light sources to avoid the influence of ambient light on facial expressions is now being considered.

There are two main targets for future research in the field of human facial analysis. One is the identification of individual human faces and the other is the analysis of human facial expressions. In the former, conventional methods have been applied to obtain facial features from a stationary face. However, if the face moves, the person cannot be identified by the conventional methods. Using the proposed method, 3D shapes are measured from a moving human face and several facial features can be obtained easily from the measured 3D data. Hence, the proposed method can be used to identify a person correctly. In the latter, conventional methods are used to analyze human facial expressions by obtaining a few features from the moving face, such as the shapes of the eyes, eyebrows, and mouth. To analyze subtle human facial expressions, it is necessary to obtain detailed shapes, such as wrinkles on the cheeks and forehead. The proposed method can be used to measure detailed 3D shapes over the complete facial
region and can be applied to the analysis of subtle changes in human facial expressions.

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